



## Search for the quadrupolar instability in URu<sub>2</sub>Si<sub>2</sub>

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### Abstract

We have performed the thermal expansion  $\alpha(T)$  and elastic constant  $c(T)$  measurements of the heavy electron system URu<sub>2</sub>Si<sub>2</sub>, with special attention to the tetragonal symmetry of  $\Gamma_3(x^2 - y^2)$  and  $\Gamma_4(xy)$ . The experimental results of  $c_{66}$ ,  $\frac{1}{2}(c_{11} - c_{12})$  and  $\alpha(T)$  along  $[\pm 110]$  do not confirm a sizable uniform distortion for these two types of symmetry through a puzzling phase transition at  $T_0 = 17.5$  K. On the other hand, the  $\frac{1}{2}(c_{11} - c_{12})$  data, which are missing in the previous detailed study, are found to show a weak but significant tendency of softening below about 70 K, suggesting an elastic response of the quadrupolar moment of  $J_x^2 - J_y^2$ .

**Keywords:** URu<sub>2</sub>Si<sub>2</sub>; Quadrupolar instability; Thermal expansion; Elastic constants

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One of the most attractive issues regarding the heavy-electron (HE) superconductor URu<sub>2</sub>Si<sub>2</sub> is to clarify the intrinsic order parameter (OP) of the phase transition at  $T_0 = 17.5$  K. Polarized neutron analyses have evidenced that 5f spin dipoles form an antiferromagnetic (AF) arrangement below  $T_0$ , excluding other prospective multipoles out of the primary OP [1]. Nevertheless, the extremely small amplitude of the observed staggered moments ( $\mu_0 \sim 0.04 \mu_B$ ), which obviously contradicts large anomalies seen in the macroscopic property, still motivates us to search for a hidden mechanism of this phase transition [2].

Instead of the tiny dipolar ordering, a quadrupolar ordering [3] and an intermediate to 5f<sup>2</sup> valence transition [4] have been argued as possible candidates for a hidden primary OP. The quadrupolar model gives a most convincing explanation to the

macroscopic property of the system, although the tiny dipolar moments must be put aside as an unknown side effect. In the valence transition model, on the other hand, the tiny moments are ascribed to an admixture of a nonmagnetic state in 5f<sup>2</sup> to excited spin states in 5f<sup>1</sup> or 5f<sup>3</sup>. The order parameter is predicted to be a gap energy between two lower-lying crystalline electric field (CEF) singlets in the 5f<sup>2</sup> configuration, which are merged with each other by valence fluctuations above  $T_0$ .

Interestingly, both models predict a lattice distortion in the tetragonal symmetry of  $\Gamma_3(x^2 - y^2)$  or  $\Gamma_4(xy)$  to be involved in the phase transition, although no direct observation has been reported yet. The purpose of this paper is to investigate such possibility of lattice instability, supplementing the data of thermal expansion and elastic constants for the relevant symmetry.

A high-quality single-crystalline bar of URu<sub>2</sub>Si<sub>2</sub> was prepared by the Czochralski tri-arc technique and no further heat treatment was performed. Two

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parallelepipeds were cut from the bulk crystal by means of high-precision spark erosion, in the orientation of  $[100]-[010]-[001]$  (corresponding dimensions  $4.0 \times 2.0 \times 2.5 \text{ mm}^3$ ) and of  $[110]-[-110]-[001]$  ( $3.0 \times 2.0 \times 2.8 \text{ mm}^3$ ). The coefficient of linear thermal expansion  $\alpha = L^{-1} dL/dT$  was measured by a sensitive three-terminal capacitance technique in the temperature range 4.2–50 K. The ultrasonic velocity  $v$  was measured with a phase comparison method in the temperature range 4.2–150 K, using piezoelectric  $\text{LiNbO}_3$  plates as ultrasonic transducers with resonance frequencies of 15 MHz (10 MHz) for longitudinal (transverse) waves. The absolute value of elastic constants  $c = \rho v^2$  was calculated with the mass density at room temperature;  $\rho \sim 10.01 \text{ g/cm}^3$ .

First, we investigate the uniform lattice distortion in the  $\Gamma_4$  symmetry by the thermal expansion along  $[110]$  directions. Previous results along  $a$  and  $b$  axes ( $\alpha_{[100]}$ ) have evidenced that there is no lattice distortion uniform in the  $\Gamma_3$  symmetry within the accuracy of  $\Delta l/l < 10^{-7}$  [5]. This geometry of experiments however is insensitive to the  $\Gamma_4$  distortion, since this distortion leads to an equivalent change in the capacitance gap for two  $[100]$  arrangements of the sample. If the  $\Gamma_4$  distortion takes place, we would detect it most clearly by  $\alpha_{[110]}$  as opposite variations between two orthogonal  $[\pm 110]$  directions. However, the amplitude of such an anomaly estimated from the  $\alpha_{[100]}$  data is equal to  $\sim 10^{-5}$  in  $\Delta l/l$ . This may nearly be of the resolution limit in other techniques, and thus it is of interest to be checked by high-precision dilatometry. The results are shown in Fig. 1. The  $\alpha_{[110]}$  data for two  $[\pm 110]$  directions are superposed not only upon each other but also with the previous results of  $\alpha_{[100]}$  [5]. We thus conclude that there is no sizable effect ( $\Delta l/l < 10^{-7}$ ) in lowering the fourfold symmetry of  $\text{URu}_2\text{Si}_2$  macroscopically.

In Fig. 2, we provide an overview of the temperature variations of elastic constant for three modes,  $c_{11}$ ,  $c_{66}$  and  $\frac{1}{2}(c_{11} - c_{12})$ . Detailed studies have already been made for the former two modes [6], while the mode  $\frac{1}{2}(c_{11} - c_{12})$  was measured for the first time. We found that this transverse mode decreases as the temperature drops, showing a maximum centered at  $T_{\text{max}} \sim 70 \text{ K}$ . Upon further

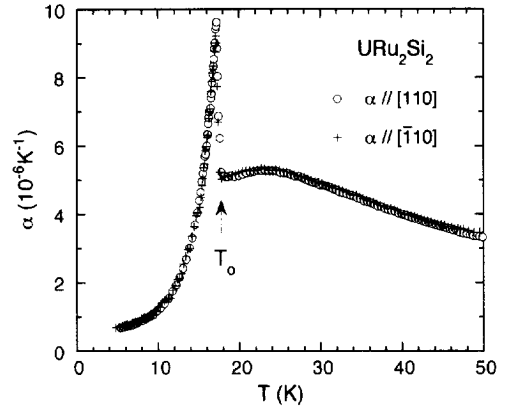


Fig. 1. The thermal-expansion coefficient along two orthogonal directions  $[\pm 110]$  of  $\text{URu}_2\text{Si}_2$ .

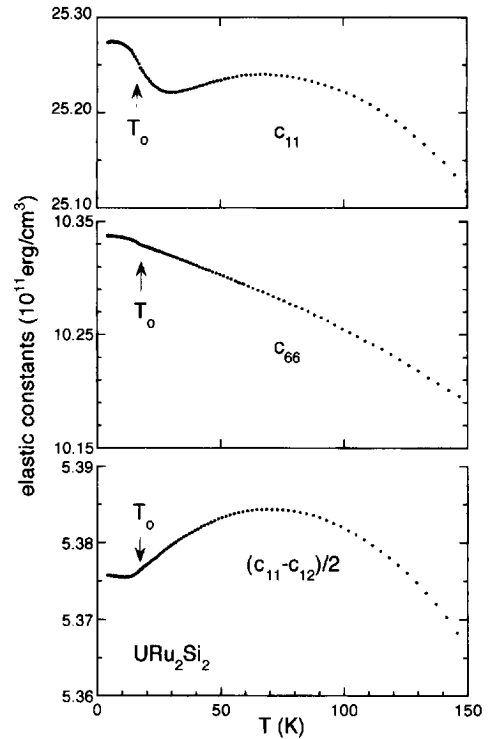


Fig. 2. Temperature variations of three elastic modes,  $c_{11}$ ,  $c_{66}$ , and  $\frac{1}{2}(c_{11} - c_{12})$  of  $\text{URu}_2\text{Si}_2$ .

cooling, it exhibits a small kink at  $T_0$  and turns up slowly again below  $\sim 12 \text{ K}$ . The data for  $c_{11}$  and  $c_{66}$  modes, on the other hand, trace the previous results qualitatively:  $c_{66}$  monotonously increases as

the temperature drops, and  $c_{11}$  exhibits a maximum at  $\sim 70$  K, followed by a broad minimum at  $\sim 30$  K.

The softening observed in  $\frac{1}{2}(c_{11} - c_{12})$  below  $T_{\max} \sim 70$  K is weak ( $\sim 0.2\%$ ) but could be remarkable in the sense that it occurs in the volume conserving transverse mode in the HE states. In general, the elastic property of HE materials can be characterized by a tendency of softening in the longitudinal modes in accordance with the volume effects due to c-f hybridization. In the previous reports [6], in fact, the anomalous behavior of the longitudinal  $c_{11}$  mode is treated in this line, since there is no anomaly visible in the transverse  $c_{44}$  and  $c_{66}$  modes. Our experiments, however, reveal a similar maximum appearing in the other transverse mode  $\frac{1}{2}(c_{11} - c_{12})$  with nearly the same relative amplitude and  $T_{\max}$  as those in  $c_{11}$ . Since  $c_{11}$  is the response to the combined strain  $\epsilon_{\Gamma_1} + \epsilon_{\Gamma_3}$ , we strongly suggest that the broad peak in  $c_{11}$  should be identical to that in  $\frac{1}{2}(c_{11} - c_{12})$  belonging to the  $\Gamma_3$  symmetry. The residual increase of  $c_{11}$  below  $\sim 30$  K might be due to the behavior in  $\Gamma_1$  symmetry, and/or due to the isothermal sound propagation as pointed out in Ref. [6]. We would like to stress that this transverse mode anomaly of  $\text{URu}_2\text{Si}_2$  gives a particularly strong contrast to the isostructural HE material  $\text{CeRu}_2\text{Si}_2$  [7] that exhibits a softening only in the longitudinal modes. This implies an essential difference in f states between these two compounds.

Assuming 5f electrons to be well localized, we could attribute the softening in  $\frac{1}{2}(c_{11} - c_{12})$  to thermal fluctuations of quadrupolar moments  $J_x^2 - J_y^2$  in the CEF 5f states. In terms of the proposed CEF quadrupolar model [3], the  $\frac{1}{2}(c_{11} - c_{12})$  data can be well described as a Van Vleck type of contribution to the strain susceptibility [8]. The absence of anomaly in the longitudinal  $c_{33}$  mode [6] is also consistent with the absence of coupling by  $J_z^2$  between lower-lying CEF states. In this view, however, the possible quadrupolar ordering must form an AF type of structure because of the above discussion on  $|\alpha_{11} \ 1 \ 0\rangle$ , and because none of transverse modes tends to diverge at  $T_0$ . On the contrary, the CEF scheme for the induced dipolar ordering [9] seems unlikely to reproduce all modes consistently, because of the opposite selection rules assumed:

a strong coupling for  $J_z^2$  but none for  $J_x^2 - J_y^2$  between lower-lying levels.

The data for  $\frac{1}{2}(c_{11} - c_{12})$  may also be consistent with the model of intermediate to  $5f^2$  valence transition [4], in the qualitative sense that the system should have the structural instability in the symmetry of  $\Gamma_3$  or  $\Gamma_4$ . Detailed calculations for the strain susceptibility in the paramagnetic intermediate states would be desirable.

In conclusion, we have discussed the lattice instability for  $\text{URu}_2\text{Si}_2$ , focusing our attention on the symmetry of  $\Gamma_3$  and  $\Gamma_4$ . Absence of uniform distortion for these two types of symmetry has been most accurately confirmed by means of dilatometry. The elastic response has been found to exhibit a tendency of softening in the symmetrized transverse mode  $\frac{1}{2}(c_{11} - c_{12})$ , suggesting the presence of lattice instability in the  $\Gamma_3$  symmetry. Such anomaly in the volume conserving mode is quite rare in HE materials and thus expected to offer the key to an understanding of the 17.5 K phase transition. Within the existing theories, the observed elastic property is consistent with the quadrupolar model, and with the valence transition model, although further analyses need to be made. To further elucidate the relation between this elastic anomaly and the ground state, the systematic analyses for the doped materials, such as  $\text{U}(\text{Ru}, \text{Rh})_2\text{Si}_2$  and  $(\text{Th}, \text{U})\text{Ru}_2\text{Si}_2$ , are planned.

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